

# Greatest Permutation

## Problem ID: greatestpermutation

A permutation with  $n$  elements is a rearrangement of the first  $n$  positive integers. For example, if  $n = 3$ , there are 6 permutations:  $(1, 2, 3)$ ,  $(1, 3, 2)$ ,  $(2, 1, 3)$ ,  $(2, 3, 1)$ ,  $(3, 1, 2)$  and  $(3, 2, 1)$ . A **great permutation** is a permutation with  $n$  elements with the form  $i, i+1, i+2, \dots, n, 1, 2, \dots, i-1$ . In other words, a great permutation can be obtained by moving a prefix of  $1, 2, \dots, n$  to its right. Please note that  $1, 2, \dots, n$  is also a great permutation.

For a permutation, let's define its **weight** as the minimum number of times you need to swap two consecutive elements, so that the permutation becomes a great permutation.

For example, the weight of  $3, 2, 1, 4$  is 2, because you can make it a great permutation after a minimum of two swaps:

- Swap the 1st and 2nd element:  $2, 3, 1, 4$ ,
- Swap the 3rd and 4th element:  $2, 3, 4, 1$ .

You are given a sequence representing a permutation with some missing elements. You need to calculate the **minimum weight** among all permutations which can be obtained by replacing missing elements with certain values. For example, given the sequence  $2, 3, 0, 0$ , where 0s denote missing elements, two possible permutations are  $2, 3, 1, 4$  with weight 1 and  $2, 3, 4, 1$  with weight 0. So the minimum weight is 0.

## Input

The first line of the input contains a single integer  $t$  — the number of test cases.  $t$  test cases follow, each test case is described as below:

- The first line contains a single integer  $n$  ( $1 \leq n \leq 10^6$ ) — the number of elements of the given permutation.
- The second line contains  $n$  space-separated integers  $a_1, a_2, \dots, a_n$  ( $0 \leq a_i \leq n$ ). It is guaranteed that you can get at least one valid permutation after changing all 0s to other values.

The sum of  $n$  in all test cases does not exceed  $10^6$ .

## Output

For each test case, print the result in a single line.

| Sample Input 1                    | Sample Output 1 |
|-----------------------------------|-----------------|
| 2<br>4<br>3 2 1 4<br>4<br>2 3 0 0 | 2<br>0          |